

# AMT 1.0: the toolbox for reproducible research in auditory modeling

Piotr Majdak, Clara Hollomey, Robert Baumgartner

The auditory modeling toolbox (AMT) is a Matlab/Octave toolbox for the development and application of auditory computational models with a particular focus on binaural hearing. The AMT aims for a consistent and structured implementation of auditory models, well-structured in-code documentation, inclusion of auditory data required to run the models, ability to reproduce the model predictions, and user-friendly access in order to allow students and researchers to work with and to advance existing models. Model implementations can be evaluated in two stages, by running so-called demonstrations which are quick presentations of a model and by starting so-called experiments aimed at reproducing results from the corresponding publications. The AMT 1.0 includes over 50 models and is freely available as an open-source package from [www.amtoolbox.org](http://www.amtoolbox.org).

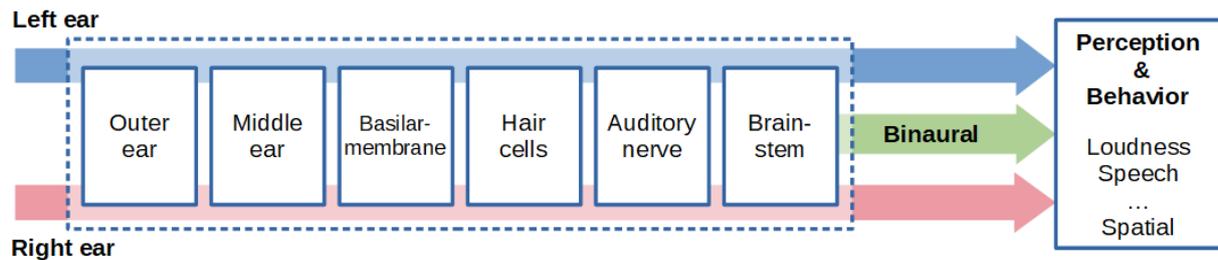
# 1. Introduction

Our understanding of the world relies on observations. These observations drive the development of models and models explain the world [1]. In the domain of hearing research, auditory models are informative representations of processes describing the hearing system. Auditory models of conceptual nature qualitatively describe behavioral or neural outcomes. Computational models usually build upon such conceptual models and consist of algorithms designed to numerically process sound stimuli and to output a measurable quantitative metric [2]. Computational models are extremely important to reproduce results and confirm conclusions [3]. In this article, we describe the auditory modeling toolbox (AMT) version 1.0, which is a collection of computational models of the human hearing system with the focus on reproducible research.

The motivation for the development of auditory models is widely spread. Auditory models can help to evaluate how a deficit in one or more components affects the overall operation of the hearing system. They also can be useful in technical applications, such as the improvement of human-machine communication, as well as in clinical applications, such as the development of new processing strategies in hearing-assistive devices. An important property of auditory models is to represent results from an auditory experiment in order to explain the functioning of the targeted part of the auditory system. To this end, new auditory models are based on already existing ones, and the development of an auditory model begins with the process of comprehending and reproducing results of previously published models [4].

Unfortunately, when a new model is published in the usual form of a journal article, the model description and discussion about its properties is often not sufficient to reproduce the results. In addition, publishing the corresponding model implementation, i.e., a computer-readable sequence of commands to be executed, is required to ensure direct reproducibility. Thus, it is not surprising that articles describing computational algorithms have been sometimes described as “advertisement of scholarship” [5] whereas the scholarship itself is then represented by computer-executable code, input data, and parameters [6]. Hence, the spectrum of reproducibility is wide [7] – model implementations linked with the corresponding publication and data are vital prerequisites for a full replication of the research [8]. The AMT directly addresses the full research replication by providing executable code and data, both linked to extensive documentation referencing the corresponding publications (see Sec. 5).

Computational models of auditory processes can focus on various levels of details. For example, there are physiological models based on the description of cochlear mechanics or neural firing mechanisms. On the other end of the spectrum, there are phenomenological (or functional) models which describe an input-output relation by a high-level function without a strict relation to the underlying bio-



**Figure 1:** Functional structure of the AMT with stages reflecting the monaural processing stages of the auditory periphery (Left ear, Right ear), followed by an optional stage of binaural interaction (Binaural) and stages modeling perceptual or even behavioral outcomes (Perception & Behavior).

49 logical structures. Most computational auditory models follow a common functional structure in line  
 50 with the ascending auditory pathway, which is reflected in the AMT in the way shown in Fig. 1: The  
 51 sound entering and filtered by the outer ear is transmitted by the middle ear, frequency-decoded in the  
 52 cochlea, neurally encoded by hair cells, transmitted via auditory nerves, and monaurally processed in  
 53 the first nuclei of the brainstem. The monaural output of those nuclei is combined with that coming  
 54 from the other ear (**Binaural** in Fig. 1). All three representations, from the left ear, the right ear, and  
 55 the binaural stage are further processed in higher-level stages dealing with the modeling of perception  
 56 and behavior. In the AMT, various types of models deal with various types of percepts such as loud-  
 57 ness, speech, or space.

58 There are many auditory models with publicly available implementations. For example, ModelDB,  
 59 one of the websites storing and listing computational neuroscience models [9], lists 65 implementa-  
 60 tions for the search word “auditory”. While model sharing is common in the neuroscience community  
 61 [10], most of the implementations focus on specific properties or stages of the auditory system, such  
 62 as modeling the frequency selectivity in cochlear processing [11] or brainstem activities [12]<sup>1</sup>, respec-  
 63 tively. Other types of implementations simulate multiple parts of the auditory pathway such as pro-  
 64 cessing up to the auditory nerve [13]<sup>2</sup>, [14]<sup>3</sup>, auditory-cortical processing [15]<sup>4</sup>, or everything relevant  
 65 to a specific percept such as loudness [16]<sup>5</sup>.

66 In contrast, the AMT is a *collection of auditory* models. It is implemented within the environment  
 67 of Matlab [17] and Octave [18]. Besides the AMT, there are also other publicly available auditory  
 68 model collections. The Auditory Toolbox is one of the earliest freely available collections and in-  
 69 cludes three cochlear models [19]. It is written for Matlab, but the development seems to have stopped  
 70 in 1993. AIM [20] is a collection of models aiming to describe the formation of auditory events along  
 71 the auditory pathway. Its development started in 1995 and the maintenance lasted until 2011 and 2013

1 <https://www.urmc.rochester.edu/labs/carney/publications-code/auditory-models.aspx>  
 2 <https://github.com/HearingTechnology/Verhulstetal2018Model>  
 3 <https://www.ece.mcmaster.ca/~ibruce/zbcANmodel/zbcANmodel.htm>  
 4 <http://nsl.isr.umd.edu/downloads.html>  
 5 <https://www.psychol.cam.ac.uk/files/tv2018matlab.zip>

72 for the offline and real-time version, respectively. Other notable but stagnated collections of auditory  
73 models are the HUTear [21] (developed until 2000), SOMA (until 2011)<sup>6</sup>, EarLab [22] (until 2016),  
74 and Cochlea [23] (until 2017). DSAM is a potentially still maintained model collection that includes  
75 multiple auditory nerve models, neural cell models, and utilities [24]. While the main development  
76 happened before 2013, some activities on re-writing the code to C++ have been restarted in 2020.<sup>7</sup>  
77 Brian Hears, a collection of cochlear models [25], was developed until 2011 and has been recently up-  
78 graded to Brian2Hears and ported to be based on Brian2, an open-source simulator for spiking neural  
79 networks being under active development [26]. At its current development, Brian2Hears includes au-  
80 ditory models developed with a focus on computational efficiency.<sup>8</sup> Most of the auditory models from  
81 all those collections are also available in the AMT, which is under long-term active development and  
82 aims as a one-stop shop for auditory models within multiple programming environments (see  
83 Sec. 2.2) and offered under multiple licenses (see Sec. 5.2).

84 Besides these general collections, there are also collections of auditory models wrapped up for spe-  
85 cial applications. Examples of such collections are Eidos that targets speech analysis [27] or Two!Ears  
86 that targets the simulation of robotic hearing including basic cognitive functions [28]. As an interest-  
87 ing side note, the Two!Ears toolbox is based on an early version of the AMT, demonstrating the im-  
88 portance of freely available and reproducible implementations of auditory models.

89 Beginning with the first AMT release (the version 0.003 released as a draft in 2010), the continu-  
90 ous contributions from the auditory community have helped us to extend the AMT. Through the AMT  
91 versions 0.x (described in [29] and released between 2013 and 2020), the AMT has matured to a large  
92 collection of auditory models. The release of the AMT 1.0 offers new features and important struc-  
93 tural changes. In this article, we describe the AMT as of the version 1.0, referring to it as the AMT.  
94 Following the semantic versioning<sup>9</sup>, this description applies to all future AMT 1.x versions. In the  
95 next sections, we describe the environment of the AMT, the available models, their tools and status,  
96 and general information such as the documentation system. Finally, we provide some practical tips for  
97 getting started to work with and contribute to the AMT.

## 98 2. Environment

99 The AMT has been developed within the environment of Matlab 2016a [17] and Octave 6.2 [30].  
100 Figure 2 shows the logical structure of the AMT. The auditory models are embedded in model-inde-  
101 pendent resources such as core functions, common functions, a caching mechanism, and access to

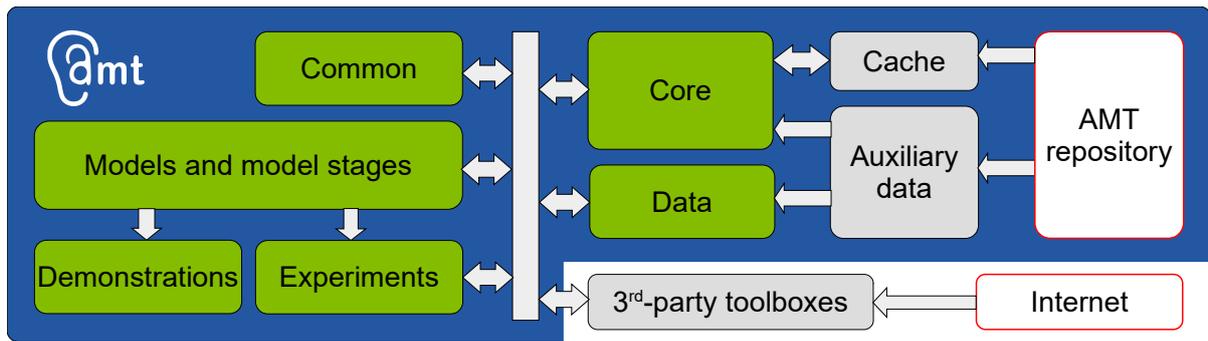
---

6 <https://code.soundsoftware.ac.uk/projects/soma>

7 <https://sourceforge.net/p/dsam/git/ci/1619b6db26b0b862c5c323c75e1fed630df2e8fd/>

8 <https://brian2hears.readthedocs.io/en/stable/index.html>

9 <https://semver.org/>



**Figure 2:** Logical structure of the AMT. **Green:** Code consisting of functions and algorithms. **Grey:** Data. **White:** Information available online for download.

102 auxiliary data with an online data repository. Further, the AMT uses various third-party toolboxes,  
 103 mostly to accommodate individual model requirements.

## 104 2.1. Core functions

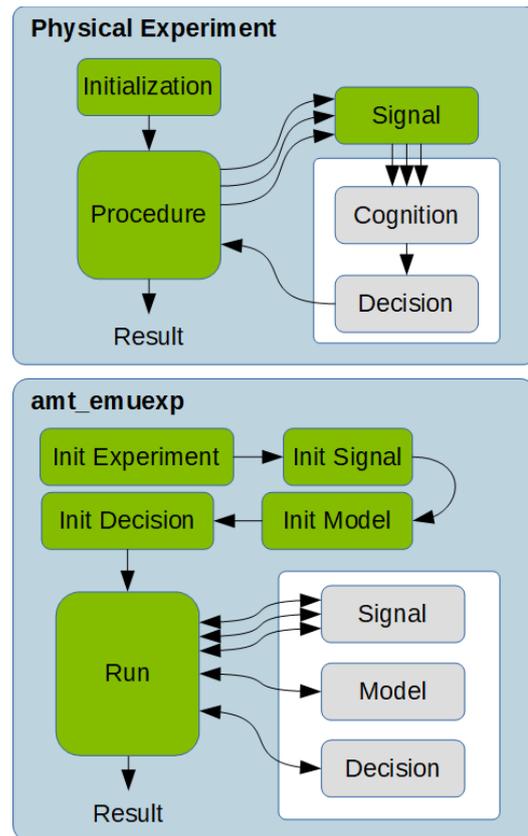
105 The core functions control the configuration and the workflow of the AMT. The most essential func-  
 106 tion is `amt_start` that installs toolboxes when required and sets up a default configuration for the  
 107 work with other AMT functions. This function supports flags to control the global behavior of the  
 108 AMT such as the behavior of the cache (see Sec. 2.3) and the message display control. For example,  
 109 when the AMT is started in the default `verbose` mode, messages will always be displayed. When the  
 110 AMT is started in the `silent` mode instead, display of all messages will be suppressed.

111 The AMT configuration can be retrieved with `[f, k]=amt_configuration`, where `f` returns the  
 112 configuration flags and `k` returns the status, paths of toolboxes (see Sec. 2.2), base path of the AMT,  
 113 paths of auxiliary data (see Sec. 2.4) and cache (see Sec. 2.3), as well as names of the current and pre-  
 114 vious AMT versions. The configuration can be displayed by calling `amt_info`. The flags can also be  
 115 obtained by the function `amt_flags`. Most of the configuration parameters can also be obtained by  
 116 the functions `amt_basepath`, `amt_auxdatapath` and `amt_auxdataurl`, `amt_cache`, and  
 117 `amt_version`. The AMT can be stopped with `amt_stop`, which removes the configuration from the  
 118 system, but does not delete the user's variables.

119 The AMT core function `amt_emuexp` provides a functionality to emulate psychophysical experi-  
 120 ments by simulating the underlying processes. In a typical psychophysical experiment (e.g., Fig. 3,  
 121 top), after an initialization of the procedure, signals are generated and provided to a subject. Then, the  
 122 subject processes them and based on cognitive mechanisms provides a decision. This decision triggers  
 123 the procedure to continue with the experiment until it finishes with a result. The function  
 124 `amt_emuexp` emulates all those components (Fig. 3, bottom). The initialization phase consists of set-  
 125 ting up `amt_emuexp` by separately providing parameters for the experiment, signal generation, audi-  
 126 tory model, and decision stage. Each of the four initializations are triggered by calling `amt_emuexp`

127 with the corresponding `init` parameter. The experiment  
 128 is started by calling `amt_emuexp` with the `run` parameter.  
 129 Then, signals are generated, their processing by the  
 130 auditory model is triggered, and the model outputs are  
 131 provided to the decision stage. The decision output trig-  
 132 gers the `amt_emuexp` procedure to continue with the  
 133 simulation until it finishes with a result. Note that func-  
 134 tions for creating the signals, modeling the auditory sys-  
 135 tem, and providing the decision are not part of the  
 136 `amt_emuexp` and can be any functions of the AMT en-  
 137 vironment. An example of using `amt_emuexp` can be  
 138 found in `demo_breebaart2001` demonstrating a  
 139 three-alternative forced choice experiment from [31].  
 140 The functionality of `amt_emuexp` also supports emulat-  
 141 ing experiments following the interface proposed in  
 142 [32]. This interface integrates the experiment software,  
 143 an auditory pathway model, and task-dependent deci-  
 144 sion stages – on potentially remote computers irrespec-  
 145 tive of their underlying programming language. In  
 146 `amt_emuexp`, this mode is initiated by initializing the  
 147 `amt_emuexp` experiment with the parameter  
 148 `interface` set to `ModelInitiative`. An example of  
 149 performing an experiment using the model initiative of  
 150 [32] can be found in `exp_breebaart2001` replicating  
 151 Fig. 3 from [31].

152 The AMT core function `amt_disp` is used for dis-  
 153 playing text in the command window, specifically tar-  
 154 geting the AMT configuration. It is an obligatory re-  
 155 placement for Matlab’s built-in function `disp`. When  
 156 called without further flags, `amt_disp` outputs the  
 157 message in a similar way to `disp`, with the behavior depending on the global verbose mode of the  
 158 AMT (see details of `amt_start` for further explanation on the start-up configurations). When called  
 159 with the parameter `volatile`, progress can be displayed in loops, i.e., by calling  
 160 `amt_disp(..., 'volatile');` in a loop and calling `amt_disp();` after the loop. For messages



**Figure 3:** Example of a typical psychophysical experiment (top) and its emulation within the AMT (bottom). **Top:** Physical experiment with an initialization the main procedure triggering signal generation provided to the subject, who receives the signals, processes them and provides a decision, terminating with a result after sufficient number of iterations. **Bottom:** Emulation of that experiment by `amt_emuexp`: Initialization of the corresponding components (`Init`), procedure stage (`Run`) controlling the signal generation, modeling the cognition, triggering the decision stage, and calculating the result. **Green:** integral parts of the experiment procedure (top) and `amt_emuexp` (bottom). **Grey:** Experiment parts representing the subject (top) and functions outside the `amt_emuexp` (bottom).

161 showing results important for the online documentation, `amt_disp` can be called with the parameter  
162 `documentation`.

163 The AMT core functions further warrant proper functioning through compilation of binaries on the  
164 user's system (`amt_mex`), calling functions from external environments (`amt_extern`), or handling  
165 recursive search within directories (`amt_subdir`), among others.

## 166 2.2. Third-party toolboxes and interfaces to external 167 environments

168 The AMT uses various third-party toolboxes and provides interfaces with other programming envi-  
169 ronments. Third-party toolboxes are packages of code developed by others independently of the  
170 AMT. They have their own but AMT-compatible license and are used by the AMT but not owned by  
171 the AMT team. These toolboxes are stored in the directory `thirdparty`. Alternatively, a user can  
172 also store them anywhere on the system and make them available within the environment's search  
173 path.

174 We distinguish between essential and model-dependent toolboxes. The large time-frequency anal-  
175 ysis toolbox (LTFAT) is an essential toolbox, which means that the AMT will not run without it. The  
176 AMT uses the LTFAT's core functions such as parsing the input parameters (LTFAT function  
177 `ltfatarghelper`) and signal-processing matrix functions such as `assert_sigreshape_pre`. If  
178 locally not available, the LTFAT will be automatically downloaded and installed. The AMT will ter-  
179minate with an error if that procedure fails.

180 The model-dependent toolboxes are not required to run the AMT, however, they are required when  
181 executing specific models. There is a variety of such toolboxes used within the AMT. For example,  
182 the application programming interface (API) for the spatially oriented format for acoustics (SOFA)  
183 handles head-related transfer functions (HRTFs) stored as SOFA files and provides general function-  
184 ality to analyze, process, and display such data [33]. In the AMT, the SOFA API is used by models  
185 requiring HRTFs. Another example is the sound field synthesis toolbox (SFS), which is used by  
186 `wierstorf2011` in order to approximate the sound field provided by loudspeaker arrays before mod-  
187 eling its auditory processing [34]. These toolboxes are provided within the AMT full release package  
188 (see Sec. 4.1).

189 The AMT supports interfaces to external environments. This way, the AMT is not limited to run  
190 models written for Matlab or Octave only – the model processing is triggered by `amt_extern` within  
191 the AMT environment, but these models are actually run outside of Matlab or Octave. These external  
192 environments can be installed anywhere on the user's system as long as they are accessible within the  
193 AMT environment. This can be done by setting corresponding paths on the user's system. Files in-

194 tended to be executed by an external environment are stored in the directory `environments`. Cur-  
195 rently, two environments are in use.

196 Models implemented in Python can be executed by calling the AMT function `amt_extern`. In the  
197 AMT 1.0, models `verhulst2012`, `verhulst2015`, and `verhulst2018` use Python version 3 in-  
198 stalled with packages `numpy` and `scipy`.

199 Models implemented in low-level programming languages such as C and C++ can be compiled to  
200 binary executable files, which are then executed on the user's machine. These files are compiled as by  
201 `amt_mex` which compiles C++ files into MEX binaries which shadow Matlab or Octave files for  
202 faster processing. These files are stored in the directory `mex` and `oct` to work in Matlab and Octave,  
203 respectively. Further, `amt_mex` executes `make.bat` and `makefile`, on Windows and Linux, respec-  
204 tively, to compile native binaries used by external environments and stored in the AMT directory  
205 `environments`. For compiling, the AMT requires the GNU compiler collection (GCC).

## 206 2.3. Cache

207 The AMT uses a two-level caching mechanism for storing pre-calculated results. The first level of the  
208 cache is locally stored in the AMT directory `cache`. That local cache has a read/write access. This  
209 means after having some data calculated, the results can be stored in that local cache and be accessed  
210 later on. The second-level cache is integrated in the online repository of the AMT, in which the cache  
211 data is stored for each AMT version separately. This online cache is read-only. Hence, the AMT can  
212 pull data from it and store it in the local cache. However, only the AMT team can push new data to  
213 the online cache. This combination of two cache levels avoids recalculations at the local level of a  
214 user and ensures a valid online cache data controlled by the AMT team. The online cache uses incre-  
215 mental versioning. Hence, only the data different from the previous version are stored.

216 The AMT cache mechanism is controlled by the function `amt_cache` that supports the commands  
217 `get` for accessing cached data as well as `set` for storing calculated data in the local cache (and further  
218 commands controlling the behavior of the cache system, see the documentation of `amt_cache`).  
219 When accessing cached data, first the data are searched in the local cache, and if not available, the on-  
220 line cache is accessed. The data are stored in the AMT's cache directory and subsequent directories  
221 named by the caller function, in files named by the user. For example, when the file `example.m` exe-  
222 cutes the command `amt_cache('set', 'xyz', a, b, c)`, the AMT will create a directory named  
223 `example` and store the variables `a`, `b`, and `c` in the file `xyz.mat`. The access to such a cached file is  
224 then given by calling `[a, b, c] = amt_cache('get', 'xyz')`. If the cached file (`xyz.mat`)  
225 does not exist, neither locally nor online, the output variables (`a`, `b`, `c`) will be empty indicating that a  
226 recalculation should be triggered. For more details, see the help section of `amt_cache`.

227 The AMT supports four global caching modes helping to control the access to the local and online  
228 repository. When calling `amt_cache` in the `normal` mode, the local cache will be used. If the data is  
229 not available in the local cache, it will be downloaded from the internet. If it is remotely not available,  
230 recalculation of the data will be enforced. Note that this method may by-pass the actual processing  
231 and thus does not always test the actual functionality of a model. It is, however, convenient for fast  
232 access of results like plotting figures. In contrast, the `redo` mode enforces the recalculation of the data  
233 without even checking the cache. In the `redo` mode, the `get` command of `amt_cache` always out-  
234 puts empty variables, triggering the recalculation. The `cached` mode is the opposite to the `redo`  
235 mode and enforces `amt_cache` to always use the cached data. If the cached data are not available,  
236 neither locally nor remotely, an error will be thrown. In the fourth cache mode `localonly`, cached  
237 results will be loaded from the local cache, but will be recalculated if locally not available. This mode  
238 is intended for running the AMT without access to the internet.

239 All these four caching modes are supported by the `get` command of `amt_cache`, allowing the user  
240 individually to force the cache behavior of specific AMT functions. For example,  
241 `exp_lindemann1986('fig6')` plots Figure 6 from [35] based on cached results, whereas  
242 `exp_lindemann1986('fig6','redo')` calculates the data and then plots that figure.

## 243 2.4. Data

244 Most of the models require data to run and test them. The AMT provides various mechanisms to ac-  
245 cess the data. We distinguish between auxiliary data, data functions, and the access to HRTFs.

246 The auxiliary data are large chunks of data that are not provided with the AMT code. This data can  
247 be accessed with the function `amt_load`. The data are retrieved from the directory `auxdata`, where  
248 they are locally stored and structured by the model name. Correspondingly, `amt_load` requires two  
249 parameters: the model and the name of the dataset. An optional third parameter can be used to load  
250 only a single variable from a larger dataset. If the requested dataset is locally not available, it will be  
251 downloaded from the AMT online auxiliary data repository, and locally stored in the AMT directory  
252 `auxdata` for future usage. Note that the local `auxdata` directory contains data for the particular  
253 AMT version only and the online `auxdata` repository contains data for each AMT version separately  
254 based on incremental versioning. Hence, only the data different from the previous version are stored.  
255 Further note that `amt_load` loads MAT files per default, but it can also be used to load audio files in  
256 WAV format, in which case, `amt_load` returns two variables: the audio data and the sampling rate.

257 Data directly referring to a publication can be accessed by the so-called data functions which have  
258 the prefix `data_`, e.g., `data_majdak2010` returns the localization responses from [36]. Data func-  
259 tions provide a more intuitive access because they can provide a documentation within the function's

260 in-code documentation and refer to the corresponding publication. Note that some of the data func-  
261 tions internally use `amt_load` to load larger chunks of auxiliary data.

262 The third data category contains HRTFs, describing the acoustic filtering of the sound by the lis-  
263 tener's body, in particular, the head, torso, and ears [37]. The AMT stores HRTFs in the directory  
264 `hrtfs` as so-called SOFA files, and uses the SOFA API for Matlab/Octave for their handling. Simi-  
265 larly to `amt_load`, the API's function `SOFAload` for loading an HRTF dataset supports caching of  
266 the HRTFs, which are, if locally not found, automatically downloaded from the AMT online HRTF  
267 repository.

## 268 2.5. Common functions

269 Common functions are helpers and converters used by models and model stages. A common function  
270 represents an algorithm with an established functionality within the auditory community, has a techni-  
271 cal background, and can be used among various models. They are not part of the AMT structural core  
272 (in contrast to `amt_core` functions), they are also not model-specific (in contrast to model stages),  
273 and they do calculations (in contrast to data functions). Common functions are stored in the directory  
274 `common` and usually created by the AMT team as soon as multiple models use a similar functionality  
275 that can be integrated to a single stand-alone function.

276 In the AMT, we have common functions that perform filter bank processing, envelope extraction,  
277 fading of signals, frequency-scale conversions, level conversions, and much more. Common functions  
278 can also calculate important parameters such as standardized hearing thresholds. In contrast to data  
279 functions, common functions perform some calculations, e.g., by interpolating or numerically evaluat-  
280 ing a formula.

281 An important property of common functions is their model independence. This is obvious when  
282 considering functions such as `sph2horpolar` that converts between spatial coordinate systems. Still,  
283 model-dependent functionality of a common auditory function can be triggered by using model-de-  
284 pendent flags. An example is `ihcenvlope` that implements a widely used model of the inner hair  
285 cell in terms of signal rectification followed by low-pass filtering. Model specific parametrization of  
286 `ihcenvlope` can be triggered by using model-specific flags supported by `ihcenvlope`. For in-  
287 stance, in order to use the inner hair cell processing with parameters from [38], the flag  
288 `ihc_bernstein1999` can be used, i.e., `ihcenvlope(insig, fs, 'ihc_bernstein1999')`.

## 289 3. Models

290 The auditory models are implemented as model functions within the AMT and have their associated  
291 model stages. Further they are accompanied by model-specific plotting functions, signal generators,

292 demonstrations, and experiments for result reproduction. Also, the status of each model implementa-  
293 tion is tracked in order to provide an estimation of the quality of the integrated models.

### 294 3.1. Models and their stages

295 In the AMT, a model is a stand-alone and testable algorithm publicly described in a scientific article  
296 discussing model parameters and providing evaluation results. Model implementations are stored as  
297 functions in the AMT directory `models`. They are named by the last name of the first author and the  
298 year of the corresponding publication, e.g., `dietz2011` for [39]. While this naming convention may  
299 appear unfair to the remaining contributing researchers, it is simple and provides great visibility to the  
300 principal author who is in most of the cases also responsible for the model implementation. If there  
301 are multiple publications with the same last name and year, a short but descriptive postfix is appended  
302 after the year, e.g., `exp_baumgartner2015binweight` distinguishes from  
303 `exp_baumgartner2015`.<sup>10</sup>

304 A model function can further depend on other functions explicitly linked with the model. These so-  
305 called model stages are usually not stand-alone, i.e., they are part of a model and they need a model in  
306 order to be tested. Only model stages belonging to a model can be included in the AMT. Model stages  
307 are stored in the directory `modelstages` and, in order to pronounce the link to the model, model  
308 stages have the prefix of the model function followed by an underscore and stage description, e.g.,  
309 `dietz2011_interauralfunctions`.<sup>11</sup>

310 For some model stages of the auditory pathway, established approaches are available and are used  
311 by a variety of other models. Such model stages do not have an explicit link to a specific model and  
312 are thus integrated as common functions, see Sec. 2.5. In the following we briefly describe models  
313 and common functions following the functional structure shown in Fig. 1.

314 The processing of the outer ear is supported by the common functions `headphonefilter`, and  
315 `hrtf2dtf`, combined with model-dependent HRTFs and the corresponding SOFA functions enabling  
316 the modeling of HRTF effects. The common function `itdestimator` collects commonly used ap-  
317 proaches to extract timing information from HRTFs, which can be checked by `ziegelwanger2014`  
318 [40] for their geometrical consistency. The transmission properties of the middle ear can be modeled  
319 by the common function `middleearfilter`.

320 Signal processing approaches to approximate cochlear processing consist of modeling the basilar  
321 membrane excitation and subsequent transmission by inner hair cells. Modeling the basilar membrane

---

10 Note the lack of underscore between the year and the postfix showing that `baumgartner2015binweight` is not part of `baumgartner2015`.

11 Note the underscore between the year and the postfix showing that `interauralfunctions` is part of `dietz2011`.

322 velocity as a function of frequency can be done by [lopezpoveda2001](#) [41], [hohmann2002](#) [42],  
323 [lyon2011](#) [11], and [verhulst2012](#) [43] as well as the common functions [auditoryfilterbank](#),  
324 [gammatone](#), [gammachirp](#), or [ufilterbankz](#). These approaches include the active feedback of the  
325 outer hair cells in various ways. The transmission of the inner hair cells is supported by the common  
326 function [ihcenvelope](#), which can be parametrized depending on the targeted behavior.

327 The auditory nerve (AN) is often linked to the models of the basilar membrane and hair cells.  
328 Hence, the models [zilany2007](#) [44], [zilany2014](#) [45], and [bruce2018](#) [14] implement the com-  
329 plete chain from sound pressure to spike rates of AN fibers. The AN functionality alone can be mod-  
330 eled with the common function [adapt loop](#) [46], which can be parametrized to simulate various ap-  
331 proaches [31, 46–49].

332 An important property of the neural auditory pathway from the cochlear nucleus to the inferior col-  
333 liculus is the sensitivity to temporal modulations, which is supported by the models [ewert2000](#) [50]  
334 and [carney2015](#) [12] as well as by the common function [modfilterbank](#) [51]. Models that also in-  
335 tegrate the more peripheral stages with some processing of higher neural stages are [dau1996](#) [46],  
336 [dau1997](#) [47], [roenne2012](#) [52], [verhulst2015](#) [53], [verhulst2018](#) [13], [relanoiborra2019](#)  
337 [48], and [king2019](#) [54]. Note that some models output individual neural spikes but others output  
338 spike rates only or even more abstract measures of neural activities.

339 Binaural processing is supported by the models [lindemann1986](#) [35], [breebaart2001](#) [31],  
340 [dietz2011](#) [55], and [takanen2013](#) [56]. The common function [itd2angle](#) further provides a sim-  
341 ple solution to create a relationship between the processed binaural timing cues and sound incidence  
342 angle.

343 The last section involves modeling various aspects of perception. In the AMT, we have loudness  
344 models represented by [moore1997](#) [57], [glasberg2002](#) [58], and [chen2011](#) [59] as well as a loud-  
345 ness model considering binaural inhibition, [moore2016](#) [60]. We have monaural speech perception  
346 models such as [joergensen2011](#) [61], [taal2011](#) [62], and [joergensen2013](#) [63] and those con-  
347 sidering binaural speech processing such as [culling2004](#) [64], [jelfs2011](#) [65], and [hauth2020](#)  
348 [66]. For perceptual similarity, we have [osses2021](#) [67] as a monaural model and [mckenzie2021](#)  
349 [68] as a binaural model. Last but not least, we have many models of spatial perception:  
350 [zakarauskas1993](#) [69], [langendijk2002](#) [70], [may2011](#) [71], [baumgartner2013](#) [72],  
351 [georganti2013](#) [73], [wierstorf2013](#) [34], [baumgartner2014](#) [74], [reijniers2014](#) [75],  
352 [kelvasa2015](#) [76], [baumgartner2016](#) [39], [hassager2016](#) [77], [baumgartner2017](#) [78],  
353 [li2020](#) [79], [baumgartner2021](#) [80], [barumerli2021](#) [81], and [mclachlan2021](#) [82]. Those  
354 models of spatial perception focus on either the direction, externalization, or distance of the sound  
355 source. The most recent models apply Bayesian inference to account for higher cognitive processes of

356 information integration across cues, modalities, and  
357 time.

## 358 3.2. Model-dependent plotting 359 and signal generation

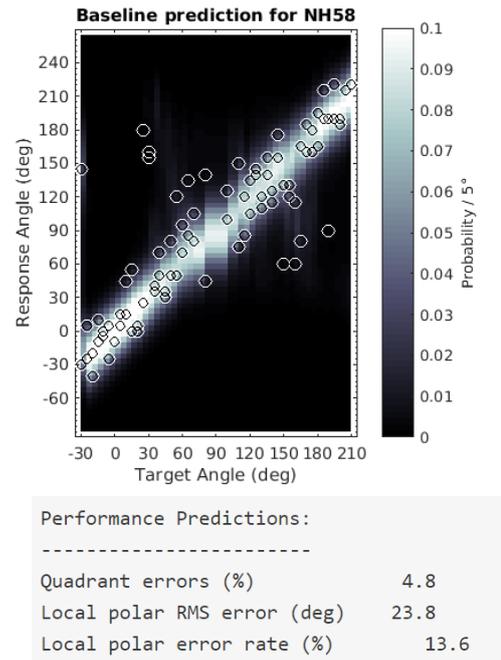
360 While Matlab and Octave provide a huge variety of  
361 functions for signal generation and plotting, the  
362 AMT provides functions specifically supporting the  
363 needs of auditory models. Signal generators have  
364 the prefix `sig_` and are stored in the `signal` direc-  
365 tory. Plotting functions have the prefix `plot_` and  
366 are stored in the `plot` directory.

367 For the file names, we follow the same pattern as  
368 for other parts of AMT functionality. Generators  
369 and plotting functions, which have been made  
370 specifically for a particular publication, have the au-  
371 thor-year identifier in their file names, e.g.,  
372 `sig_hartmann1996` generates the signals tested in  
373 [83]. Functions which are used more widely across  
374 multiple publications and represent more general  
375 plotting and signal generation, have their function-  
376 ality in the filename, e.g., `sig_ildsin` generates a binaural sine wave with an interaural level differ-  
377 ence.

## 378 3.3. Demonstrations and experiments

379 Demonstrations are scripts which can be run without any parameters in order to demonstrate the func-  
380 tionality of a model or data. Demonstrations have the prefix `demo_` and are stored in the directory  
381 `demos`. Demonstrations provide a visual representation of a model output. Figure 4 shows an example  
382 of a demonstration. Demonstrations are scripts, not functions, thus, they finish with all used variables  
383 in the user's workspace, ready to be inspected by the user for easily getting into the model's function-  
384 ality.

385 Experiments address the reproducible-research objective of the AMT. They aim at reproducing  
386 model results from publications related to the models. Ideally, they produce exactly the same results  
387 as that from the corresponding article. By visually comparing the experiment output, the quality of the  
388 model can be estimated, see the following section on the model status. Experiments are functions (not  
389 scripts) with the prefix `exp_` followed by the last name of the first author and the year of the publica-



**Figure 4:** Output of the demonstration `demo_baumgartner2014` consisting of a panel shown in a figure and alphanumeric output to the command window. **Panel:** The circles show the actual responses of the listener NH58 from [36] localizing noise bursts presented from various target angles along the median plane. Brightness encodes the probability to respond at an angle predicted by `baumgartner2014` [74]. **Text:** predicted localization performance for that listener.

390 tion reporting the simulation results. Most of the AMT's experiments are those replicating the out-  
391 come of a publication describing a model, e.g., `exp_bruce2018` replicates figures from [14] obtained  
392 by running `bruce2018`. A parameter with the prefix `fig` is used to produce a figure, e.g.,  
393 `exp_baumgartner2014('fig2')` reproduces the Fig. 2 from [74]. Prefix `tab` is used to produce a  
394 table, e.g., `exp_baumgartner2014('tab2')`.

395 In addition to the experiments replicating the model publication, further experiments replicate the  
396 outcome of secondary publications, i.e., those which apply an already published model. In the AMT,  
397 the naming convention is to use the naming of the secondary publication. At the moment of writing, in  
398 the AMT, we have only a few of such cases: `exp_baumgartner2015` replicating the outcome from  
399 [84] and `exp_baumgartner2015binweight` replicating the outcome from [85], both applying  
400 `baumgartner2014` from [74]; `exp_engel2021` from [86] applying both `reijniers2014` and  
401 `baumgartner2021`; `exp_osses2022` from [86] applying `dau1997`, `verhulst2015`,  
402 `verhulst2018`, `bruce2018`, `king2019`, `relanoiborra2019`, and `osses2021`;  
403 `exp_roettges2022` from [87] applying `hauth2020`; and `exp_steidle2019` from [88] applying  
404 `itdestimator` and `ziegelwanger2014`.

405 Experiments can also be used to pass the reproduced results to the caller functions for further pro-  
406 cessing. Their difference to the functions providing auxiliary data (`data_`) is that experiments process  
407 some data by the models, whereas the data functions just load existing data. Still, the focus of the ex-  
408 periments is to reproduce model results. If some experiment output is used frequently by others, this  
409 output is a good candidate for a transfer to a data function in the future.

### 410 3.4. Model status

411 The AMT tracks the status of each model implementation in order to provide an estimation of the  
412 quality of the models available in the AMT. The model status describes the quality of the model's  
413 source code and documentation, as well as verification. The verification considers the correspondence  
414 between the results shown in the corresponding publication and the results provided by the AMT im-  
415 plementation, usually implemented within the experiment functions.

416 The status of the code and the documentation distinguishes between four states (with letter score in  
417 brackets):

- 418 • **Submitted (D)**: The model has been submitted to the AMT team and the code has been included in  
419 the source-code repository as submitted, but it has not been integrated yet (no documentation, po-  
420 tential compilation errors, libraries missing, etc). In the release version, the model neither appears  
421 on the website nor is available for download. The current state of the integration can be provided  
422 upon request.

423 • **Satisfactory (C)**: The code/documentation fits the AMT conventions just enough for being avail-  
424 able in the release version for download. The model and its documentation appear on the website,  
425 but major work may still be required.

426 • **Good (B)**: The code/documentation follows the AMT conventions, but there are still open issues.

427 • **Perfect (A)**: The code/documentation fully complies with the AMT conventions, no open issues.

428 Note that after reaching the status “Perfect”, that model status remains even when a minor issue ap-  
429 pears (most probably raised by an AMT user).

430 The status of the verification consists of four states:

431 • **Unknown (D)**: The AMT can not run experiments for this model and can not produce any results  
432 usable for verification. This is the default state right after having a model implementation provided  
433 to the AMT team.

434 • **Untrusted (C)**: The verification code is available but the experiments do not reproduce the relevant  
435 parts of the publication. The AMT team is seeking for a solution to reveal the problems in the dis-  
436 crepancy between the publication and the implementation.

437 • **Qualified (B)**: The experiments produce similar results as in the publication in terms of showing  
438 trends and explaining the effects, but not necessarily matching the numerical results. Explanation  
439 for the differences can be provided, for example, not all original data being available, or publication  
440 being affected by a known and documented bug.

441 • **Verified (A)**: The experiments produce the same results as in the publication. Minor differences are  
442 allowed if a plausible explanation is provided, e.g., layout issues in the graphical representations or  
443 randomness introduced by noise or other probabilistic modeling approaches.

444 A table providing an overview of the available models and their status can be found on the AMT web-  
445 site<sup>12</sup>. Note that the status is only a snapshot of the development because the implementations in the  
446 AMT are continuously developed, evaluated, and improved. Any feedback is appreciated either via  
447 email or ticket created on SourceForge.

## 448 4. Working with the AMT

### 449 4.1. Getting started

450 The AMT 1.0 has been developed and tested with Matlab 2016a and Octave 6.2 under Windows 10  
451 Pro (2004) and Linux Ubuntu Focal Fossa (20.04 LTS). While most of the models will work with  
452 even older versions of Matlab and Octave, we recommend using one of the tested environments. In

---

12 <http://amtoolbox.org/>

453 addition to the pure Matlab installation, additional toolboxes, such as the “Signal processing toolbox”  
454 and the “Statistics and machine learning toolbox” may be required to run some of the models. With  
455 Matlab 2016a or later, these toolboxes can be installed by using the Add-On Explorer within the Mat-  
456 lab user interface. Similarly, when run in Octave, some models require additional packages such as  
457 `signal`, `statistics`, and `netcdf`, which need to be installed by the user before starting the AMT.

458 The AMT also requires third-party toolboxes (see Sec. 2.2). The toolboxes can be obtained in sev-  
459 eral ways. The easiest and recommended method is to use the AMT releases marked as `amttoolbox-`  
460 `full` packages, which contain all those toolboxes. With a full package downloaded and unzipped on  
461 the user’s system, `amt_start` starts the AMT.

462 The second method is to let the AMT download the toolboxes during the first start of the AMT.  
463 This is required when the non-full package of the AMT release is available. The download and tool-  
464 box installation can be then executed by `amt_start('install')`, which triggers an interactive in-  
465 quiry of the toolboxes to be downloaded and installed. Note that, if none of the toolboxes are avail-  
466 able, `amt_start` per default downloads the LTFAT and terminates with an error if LTFAT installa-  
467 tion fails because the LTFAT is an essential toolbox. But, `amt_start` does not download other tool-  
468 boxes because they are not essential to a large part of the AMT functionality.

469 The third method is the manual installation of the third-party toolboxes by the user. This method  
470 provides the most flexibility at the price of most effort and required knowledge about the user’s sys-  
471 tem.

472 Some of the AMT models need to be compiled for the particular system of the user. For users’  
473 convenience, some pre-compiled binaries are provided with the release of the AMT, however, bina-  
474 raries compiled for the user’s system may be required in some cases. This can be done by executing the  
475 command `amt_mex`, which 1) compiles corresponding Matlab/Octave files to the so-called MEX bi-  
476 naries, and 2) compiles the C and C++ files provided with the AMT to binary files. In order to run  
477 `amt_mex`, the GNU compiler collection (GCC) must be available as the command `gcc` within the  
478 AMT environment. The particular package depends on the user’s operation system and can be down-  
479 loaded from many sources on the internet. The availability can be checked by two means: 1) calling  
480 `mex -setup` shows the compiler available to compile MEX files, or 2) calling `system('gcc')` ter-  
481 minates with an error of no input files provided only if GCC is available to compile C and C++ files.  
482 Note that `amt_start('install')` also executes `amt_mex` in order to provide compiled models.

483 The AMT configuration and status of available toolboxes is handled by the command  
484 `amt_configuration` (see Sec. 2.1). Information on which toolboxes are required for running a spe-  
485 cific model can be queried by executing `amt_info` with the model name as parameter.

## 4.2. Contributing to the AMT

Each AMT user is warmly welcome to contribute to the AMT. The motivation for a contribution can be manifold. For example, an AMT user has implemented a model and wants the findings to be available and accessible for future research as this increases its potential impact. Or, an AMT user has applied a model from the AMT and has implemented experiments or demonstrations displaying the model functionality. Or, an AMT user has a general urge to support reproducible research and learn about open-source projects and auditory modeling.

In any case, we highly encourage any AMT user – before locally modifying AMT files – to retrieve the most recent version from the source repository<sup>13</sup> and integrate the modifications into that repository. This way, modifications can be uploaded to the online repository, will not be forgotten on the local computer, and can be spread among the AMT community. To this end, we recommend the following workflow (we assume a general knowledge of git, a distributed version-control system for collaborative development of software, [89]):

Retrieve the AMT repository and clone the code using `git clone https://git.code.sf.net/p/amtoolbox/code amtoolbox-code`

- Create a branch named by your last name and the year of your contribution, e.g., `smith2021` for Ms. Smith contributing in 2021. The corresponding git command would be `git branch smith2021` in that example.
- Switch to that branch, e.g., `git checkout smith2021`
- Write the code and add all your files to the repository, `git add your_files`.
- Commit your changes to your local git repository and describe the changes.

Note that by using an own branch, no harm can be done to the “official” AMT code at all.

In the next step, the modifications can be provided to the AMT team by pushing the local branch to the AMT repository. To this end, the user needs to obtain write access to the repository which is provided by the AMT team after approaching us via email. We will include the user’s SourceForge<sup>14</sup> account to the list of AMT developers, enabling the user to push the files to the online AMT repository. Then, the AMT team will review the users’ contribution aiming at integrating that contribution in the main AMT code. For contributions written in programming languages other than Matlab or Octave, the AMT team will provide the means for their integration (e.g., see Sec. 2.2). In order to make the integration of changes as smooth as possible, we ask to follow the following requirements.

---

<sup>13</sup> <https://sourceforge.net/p/amtoolbox/code/>

<sup>14</sup> <https://sourceforge.net/>

### 516 **4.2.1. Environment**

517 The AMT is aimed to be compatible with five-years old Matlab versions, i.e., Matlab 2016a for the  
518 AMT 1.0. This needs to be considered when developing and integrating own functions. Further, we  
519 aim at using as few additional dependencies as possible. When proposing a new Matlab or third-party  
520 toolbox as a requirement, we ask to check whether the required functionality is provided with the  
521 AMT and/or currently available toolboxes. When proposing an additional third-party toolbox, we ask  
522 to check whether it is freely available and its license is GPL-compatible. We also ask to check for fur-  
523 ther dependencies of those toolboxes because third-party toolboxes need to be self-contained, i.e., not  
524 depending on further toolboxes and consist of code only (no data in the toolboxes). When adding a  
525 new third-party toolbox, we ask to locally store it in the directory `thirdparty` and notify us. We  
526 will then integrate its functionality and usage within the AMT environment. Note that it is not allowed  
527 to include third-party toolboxes in the AMT code repository.

### 528 **4.2.2. Directory structure**

529 The files are stored in directories reflecting the AMT environment (see Sec. 2). For the new contribu-  
530 tion, the model implementation goes as a single function into the directory `models`. This model func-  
531 tion can be complemented by (multiple) model stages stored in the directory `modelstages`. Model-  
532 specific data, plotting functions, and signal generators go to `data`, `plot` and `signals`, respectively.  
533 Model demonstrations and experiments reproducing results go to `demos` and `experiments`, respec-  
534 tively. Large chunks of data can be locally stored as auxiliary data in `auxdata`; they need to be ac-  
535 cessed by `amt_load` and provided to the AMT team (link via email) after having the code submitted  
536 to the remote repository.<sup>15</sup> In demonstrations and experiments, if the processing duration is beyond a  
537 few minutes, we encourage to cache the results by integrating `amt_cache`.

### 538 **4.2.3. Function and file names**

539 Underscore is a reserved character in the AMT environment and used only to distinguish structural  
540 parts in the AMT. All function names are lowercase. This avoids a lot of confusion because 1) some  
541 computer architectures handle the casing with various relevance and 2) in Matlab or Octave documen-  
542 tation, function names are traditionally converted to uppercase. Function names indicate what they do,  
543 rather than the algorithm they use, or the person who programmed or invented it. For reasons pointed  
544 out earlier in Sec. 3, prominent exceptions represent the model functions and their demonstrations as  
545 well as experiments, which are named by the last name of the first author followed by the year of the  
546 corresponding publication.

547 If the new model consists of several functions, the model function contains the main functionality  
548 and the remaining parts are covered by model stages. Stand-alone model stages without a correspond-  
549 ing model are not allowed; a model stage needs a model. Local functions, i.e., functions within a file

---

15 Commit of data to the code repository is not allowed.

550 containing the main function, have the prefix `local_` in order to easily be distinguished from other  
551 AMT functions. The function `amt_disp` is used to display text in the command window, offering  
552 functionality such as volatile display of progress and pushing results to the online documentation. For  
553 the sake of simplicity, object-oriented programming and use of own classes are not recommended.

#### 554 **4.2.4. Variable names and default parameters**

555 Within each function, variable names are allowed to be both lower and upper case, depending on the  
556 author's personal style. Use of global variables is not allowed because they make the code harder to  
557 debug and to parallelize. In matrices, the first dimension is time (or the sampled time interval).

558 For the handling of default and optional parameters, we use the functionality provided by the func-  
559 tion `lftatarghelper` from the LTFAT<sup>16</sup>. When creating a new model, it is required to store all  
560 model's default parameters in a separate file placed in the directory `defaults` and named by model's  
561 name with the prefix `arg_`. This file needs to be a function with `definput` as input and output, in  
562 which flags are stored in the structure `definput.flags` and key-value pairs are stored in the struc-  
563 ture `definput.keyvals` – see arbitrary `arg_` function for more details. Then, in the model, for the  
564 parameter parsing, the function `lftatarghelper()` from the LTFAT is used in the following form:

```
565     definput.import = {'model2021'}; % load defaults from arg_model2021  
566     [f, kv] = lftatarghelper({}, definput, varargin);
```

567 resulting with flags and key-value pairs stored in the structures `f` and `kv`, respectively. Note the  
568 `varargin` input to the `lftatarghelper`, which passes the optional parameters provided to a model  
569 to be processed. This way default parameters from the `arg_` function will be overwritten by option-  
570 ally provided parameters to the model. While `lftatarghelper` supports complex passing of param-  
571 eters, in order to provide a clearly structured handling of the default parameters, we discourage from  
572 loading multiple default parameter files.

#### 573 **4.2.5. Signal levels**

574 Auditory models can be nonlinear and the numeric representation of physical quantities like the sound  
575 pressure level (SPL) must be well-defined. In the AMT, an audio signal represents sound pressure in  
576 Pascal and is represented on the logarithmic dB scale *re* 20  $\mu$ Pa. Thus, an audio signal having a root-  
577 mean square (RMS) level of 1 (e.g., a square signal with the amplitude between -1 and 1, or a sine  
578 with the amplitude between  $\pm\sqrt{2}$ ) corresponds to an SPL of 93.9794 dB. This level convention re-  
579 flects the SI system and is the default level convention in the AMT<sup>17</sup>. However, AMT models have  
580 been developed with a variety of level conventions and a level conversion is sometimes required. To  
581 this end, the AMT common function `dbspl` calculates the SPL in dB of an audio signal considering

---

16 See <http://lftat.github.io/doc/base/lftatarghelper.html>

17 Note that this is a non-compatible change with respect to the AMT 0.x.

582 the AMT level convention. While this function is similar to the Matlab/Octave function `rms`, `db SPL`  
583 additionally converts to the logarithmic dB scale and considers the AMT level convention. In some  
584 cases, an audio signal needs to be scaled to a given SPL considering the AMT level convention. This  
585 can be done with the function `out=scaletodb SPL(in, SPL)`, which scales `in` such that the SPL of  
586 `out` is `SPL`. Note that when a linear model such as the linear Gammatone filterbank is applied, the  
587 level convention can be ignored. Note further that because of historical reasons, previous AMT ver-  
588 sions used a different level convention as the default.

589 While we are happy about contributions with perfectly structured code, clear parameter passing,  
590 and naming exactly following the AMT conventions, we encourage all programmers and researchers  
591 to contribute their code *as it is* and *as soon as possible*. “Publish your code: it’s good enough” [90].

## 592 5. General information

### 593 5.1. Documentation

594 The AMT uses an in-code documentation system, i.e., the documentation text is embedded in the  
595 source-code files of the implementation. This way, a high level of integrity between the code and doc-  
596 umentation can be provided and still a human-readable documentation can be generated. When releas-  
597 ing a new AMT version, this documentation is compiled by the compiler `mat2doc`<sup>18</sup> to an offline doc-  
598 umentation available when calling `help` within the Matlab or Octave environment, e.g., `help`  
599 `exp_hassager2016`, and an online documentation published at the AMT documentation website.

600 The syntax of `mat2doc` is based on `reStructuredText`<sup>19</sup>, a widely used markup syntax and parser  
601 component of `Docutils`<sup>20</sup>. The documentation based on `reStructuredText` can be compiled online.<sup>21</sup> In  
602 `mat2doc`, relevant differences to `reStructuredText` are 1) the comment character `%` in each line, 2) the  
603 first line representing a brief description of the function, e.g.; `%AMT_CACHE Caches variables`,  
604 according to Matlab tradition, and 3) in all other lines, applying the three-blank rule between `%` and  
605 the first letter of the text, e.g., `% This is an example.`

606 In addition, `mat2doc` adds some environment-specific features triggered by keywords. The key-  
607 word `Usage:` appended by multiple lines shows how the corresponding function can be called, e.g., `%`  
608 `Usage: amt_start;`. The keywords `Input parameters:` and `Output parameters:` ap-  
609 pended by multiple lines can be used to explain the input and output parameters of a function. The  
610 keyword `References:` appended by a single-line list of BibTex<sup>22</sup> identifiers includes a list of refer-

---

18 <http://mat2doc.sourceforge.net/>

19 <https://docutils.sourceforge.io/rst.html>

20 <https://docutils.sourceforge.io/index.html>

21 <http://rst.ninjs.org/>

22 <http://www.bibtex.org/>

611 ences used to cite publications within the documentation. The corresponding references are stored in  
612 the file `project.bib` in the AMT directory `mat2doc`. The keyword `See also:` appended by a sin-  
613 gles-line list of other AMT functions includes a list of links to other relevant AMT functions. Note that  
614 these keywords must be used exactly as given, including the casing and colon.

615 Further, the in-code documentation supports the so-called anchors, which are keywords to provide  
616 additional and machine-readable information about the authors, requirements, the license, and model  
617 status (see `amt_info`). The anchors are encoded as `% #Anchor:` (three blanks between `%` and `#`)  
618 and are provided in a comment block of the in-code documentation. The author information is en-  
619 coded by the anchor `#Author` and can be provided in multiple lines (each of them beginning with  
620 `% #Author:`), enabling various author contributions over the course of time. The information  
621 about requirements uses `#Requirements` and represents the required environment (either `Matlab` or  
622 `Octave`, never both), internal packages (`M-signal` and/or `M-statistics` for Matlab toolboxes),  
623 third-party toolboxes (`SOFA`, `SFS`, and/or `CircStat`), and additionally required environments  
624 (`Python`, `Binary`, and/or `MEX`). The anchor `#License` enables the multi-licensing feature of the  
625 AMT (see the following section). The model status is encoded by the anchors `#StatusDoc`,  
626 `#StatusCode`, and `#Verification` followed by the short name of the status as enlisted in Sec. 3.4.

## 627 5.2. Licensing

628 The code written by the AMT core team is licensed under the GNU general public license (GPL) ver-  
629 sion 3, which basically allows users to run, study, share, and modify the software. Also the code writ-  
630 ten by other contributors for the AMT is licensed under GPL. By committing code to the AMT reposi-  
631 tory, contributors agree to use that license and to transfer the ownership to the AMT team.

632 While the AMT generally follows the GPL, in order to include implementations not licensed under  
633 the GPL, the AMT also supports multiple licensing. To this end, model implementations provided by  
634 the researchers and integrated in the AMT can be licensed under a license different from the GPL. A  
635 researcher may choose a separate license regulating the usage of that model, and while the author  
636 grants the AMT team the permission to distribute the model to third parties without a prior written au-  
637 thorization, the model ownership remains with the author. This information is clearly described within  
638 the corresponding files.

639 Licensing also involves third-party toolboxes. For a clear legal integration, only toolboxes with li-  
640 censes compatible for working with the GPL are used in the AMT. The license information is stored  
641 in the toolboxes' corresponding directories as provided by the toolbox authors. The ownership of  
642 third-party toolboxes remains with the toolbox authors.

643 For models deviating from GPL v3, at their first usage, the AMT displays a boilerplate, i.e., a brief  
644 note about the separate license and the most important terms such as terms of usage. That boilerplate

645 and the license type can also be displayed any time by executing `amt_info` with the model name as  
646 parameter. For example, a model can be restricted to be used in non-commercial applications only. In  
647 such a case, while the AMT is allowed to be used in commercial projects (as a consequence of the  
648 GPL), the user will be warned that by using that particular model, commercial usage is prohibited.

649 Note the difference between a model deviating from GPL v3 in the AMT and a third-party tool-  
650 box. A toolbox is integrated without any modification and the ownership remains with the authors. A  
651 model, even when integrated under a license different to GPL, requires code modifications. To this  
652 end, we seek permission from the researchers allowing us to edit and integrate their code. By having  
653 the model integrated, it has joint ownership (unless the researchers have transferred the ownership to  
654 us) and remains under the researcher's preferred license.

655 The license information is provided by the following mechanism: 1) The AMT directory  
656 `licenses` stores two plain-text files per license: the full license text and a license's boilerplate,  
657 named as `X_license.txt` and `X_boilerplate.txt`, respectively, with `X` being the short keyword  
658 describing the license; 2) File-specific information about the license by means of in-code documenta-  
659 tion, with the license anchor followed by the license keyword (casing ignored). Files without the li-  
660 cense information are licensed under the standard AMT license. For example, the `licenses` direc-  
661 tory contains the files `ugent_license.txt` as well as `ugent_boilerplate.txt` and by using  
662 `% License: UGent` in any file, that file will be licensed under the license of the University Gent.

### 663 5.3. Acknowledging researchers for their contribution

664 Development of new models is much work. And publishing the model implementation is easy via the  
665 internet. Thus, researchers may ask for the motivation to permit their work to be integrated in the  
666 AMT or even more, to even put more effort and integrate it in the AMT by themselves. To address  
667 this issue, the AMT provides a variety of ways to acknowledge researcher's work and display re-  
668 searcher's contribution.

669 First, the models are named after the last name of the first author of the publication describing the  
670 model, providing great visibility to the main author of the model. Second, the publication describing  
671 the model is clearly cited on the AMT website. This promotes the researcher and the publication be-  
672 yond the journal publisher's common promoting channels. Further, the publication describing the  
673 model is cited in the AMT in-code documentation, which is visible in both the AMT online documen-  
674 tation and within the Matlab/Octave help system. Last but not least, the models integrated in the AMT  
675 are cited by publications describing the AMT. This is an important means of scientific recognition,  
676 emphasizing the significance of the researcher's contribution to a better understanding of the auditory  
677 system.

678 Not only model developers, but also researchers applying AMT models in their publications can  
679 provide experiments reproducing their results to the AMT. The contribution of these researchers will  
680 be visible by having their own `exp_` function named by their last name and with a reference to their  
681 publication, acknowledging their effort of contributing to the AMT.

682 Finally, even programmers, neither contributing a full model nor an experiment, but improving the  
683 AMT code, get acknowledged by noting their names in the sources and online code repository. The  
684 AMT website lists all AMT contributors so far.

## 685 6. Conclusions

686 The AMT 1.0 implements over 50 auditory models and integrates eleven publication-specific and 29  
687 general datasets. It is available (with all the required third-party toolboxes) from SourceForge<sup>23</sup> as a  
688 free and open-source software package for Matlab and Octave. Most of the AMT’s models and data  
689 are well-documented and verified, as reflected in the model status of the AMT’s documentation web  
690 page<sup>24</sup>. The models are accompanied by “demonstrations” providing a simple access to a model’s im-  
691 plementation and “experiments” aiming at reproducing the models published output. An online data  
692 repository helps to keep the AMT compact, while still having access to all data required to reproduce  
693 each model’s output. The open-source code repository combined with a comprehensive documenta-  
694 tion system, multi-licensing, and contribution reward aims at helping others to contribute to the AMT  
695 at a low entry threshold.

696 With the release of AMT 1.0, the AMT has matured to a large collection of auditory models. It  
697 now includes new models such as those based on Bayesian inference, statistical signal processing, and  
698 predicting speech intelligibility. The AMT would not be that comprehensive without the many contri-  
699 butions from various researchers from the auditory community, for which we are wholeheartedly  
700 grateful.

701 By integrating comprehensive monaural processing stages with models of binaural and spatial  
702 hearing, the AMT paves the road towards more complex cognitive auditory models. Researchers from  
703 the auditory cognitive sciences are invited to pick them up and extend them towards more encompass-  
704 ing models of auditory or multimodal cognition.

## 705 7. References

1. Frigg, R., and Hartmann, S. (2012). “Models in Science,” In E. N. Zalta (Ed.), *Stanf. Encycl. Philos.* Fall 2012.
2. Meddis, R., Lopez-Poveda, E., Fay, R. R., and Popper, A. N. (Eds.) (2010). *Computational Models of the Au-*

---

23 <https://sourceforge.net/projects/amtoolbox>

24 <http://amtoolbox.org/>

*ditory System*, Springer Handbook of Auditory Research Springer US.

3. Jasny, B. R., Chin, G., Chong, L., and Vignieri, S. (2011). “Again, and Again, and Again ...,” *Science* **334**, 1225–1225.
4. Vandewalle, P., Kovacević, J., and Vetterli, M. (2009). “Reproducible research in signal processing: What, why, and how,” *IEEE Signal Process. Mag.* **26**, 37–47.
5. Schwab, M., Karrenbach, N., and Claerbout, J. (2000). “Making scientific computations reproducible,” *Comput. Sci. Eng.* **2**, 61–67. Presented at the Computing in Science Engineering.
6. Mesirov, J. P. (2010). “COMPUTER SCIENCE Accessible Reproducible Research,” *Science* , doi: 10.1126/science.1179653.
7. Peng, R. D. (2011). “Reproducible Research in Computational Science,” *Science* **334**, 1226–1227.
8. Claerbout, J. F., and Karrenbach, M. (1992). “Electronic documents give reproducible research a new meaning,” *SEG Tech. Program Expand. Abstr. 1992*, SEG Technical Program Expanded Abstracts Society of Exploration Geophysicists, Vols. 1-0, pp. 601–604.
9. Peterson, B. E., Healy, M. D., Nadkarni, P. M., Miller, P. L., and Shepherd, G. M. (1996). “ModelDB: an environment for running and storing computational models and their results applied to neuroscience,” *J. Am. Med. Inform. Assoc. JAMIA* **3**, 389–398.
10. Morse, T. M. (2007). “Model sharing in computational neuroscience,” *Scholarpedia* **2**, 3036.
11. Lyon, R. (2011). “Cascades of two-pole–two-zero asymmetric resonators are good models of peripheral auditory function,” *J Acoust Soc Am* **130**, 3893–3904.
12. Carney, L. H., Li, T., and McDonough, J. M. (2015). “Speech Coding in the Brain: Representation of Vowel Formants by Midbrain Neurons Tuned to Sound Fluctuations,,” *eNeuro* , doi: 10.1523/ENEURO.0004-15.2015.
13. Verhulst, S., Altoè, A., and Vasilkov, V. (2018). “Computational modeling of the human auditory periphery: Auditory-nerve responses, evoked potentials and hearing loss,” *Hear. Res., Computational models of the auditory system* **360**, 55–75.
14. Bruce, I. C., Erfani, Y., and Zilany, M. S. A. (2018). “A phenomenological model of the synapse between the inner hair cell and auditory nerve: Implications of limited neurotransmitter release sites,” *Hear. Res., Computational models of the auditory system* **360**, 40–54.
15. Ru, P. (2001). *Multiscale Multirate Spectro-Temporal Auditory Model* (PhD Thesis), University of Maryland College Park.
16. Moore, B. C. J. (2014). “Development and Current Status of the ‘Cambridge’ Loudness Models,” *Trends Hear.* **18**, 2331216514550620.
17. Higham, D. J., and Higham, N. J. (2016). *MATLAB guide*, Siam, Vol. 150.
18. Eaton, J. W., Bateman, D., and Hauberg, S. (2002). *GNU Octave Manual*, Network Theory, Ltd.
19. Malcolm Slaney (1998). *Auditory Toolbox: A MATLAB Toolbox for Auditory Modeling Work* (No. #1998-010), Interval Research Corporation.
20. Patterson, R. D., Allerhand, M. H., and Giguère, C. (1995). “Time-domain modeling of peripheral auditory processing: a modular architecture and a software platform,” *J. Acoust. Soc. Am.* **98**, 1890–1894.
21. Härmä, A., and Palomäki, K. (1999). “HUTear - A Free Matlab Toolbox for Modeling of Human Auditory

- System,” Presented at the Matlab DSP Conference, 96–99.
22. Mountain, D. C., Anderson, D. A., Bresnahan, G. J., Deligeorges, S. G., Hubbard, A. E., and Vajda, V. (2006). “EarLab: A modular approach to auditory simulation,” *J. Biomech., Abstracts of the 5th World Congress of Biomechanics* **39**, S434.
  23. Rudnicki, M., Schoppe, O., Isik, M., Völk, F., and Hemmert, W. (2015). “Modeling auditory coding: from sound to spikes,” *Cell Tissue Res.* **361**, 159–175.
  24. O’Mard, L. P. (2012). *Development System for Auditory Modelling (DSAM)*, Centre for the Neural Basis of Hearing (CNBH).
  25. Fontaine, B., Goodman, D. F. M., Benichoux, V., and Brette, R. (2011). “Brian Hears: Online Auditory Processing Using Vectorization Over Channels,” *Front. Neuroinformatics* , doi: 10.3389/fninf.2011.00009.
  26. Stimberg, M., Brette, R., and Goodman, D. F. (2019). “Brian 2, an intuitive and efficient neural simulator,” *eLife* **8**, e47314.
  27. Gutkin, A. (2020). “Eidos: An Open-Source Auditory Periphery Modeling Toolkit and Evaluation of Cross-Lingual Phonemic Contrasts,” *Proc. 1st Jt. Workshop Spok. Lang. Technol. -Resour. Lang. SLTU Col- lab. Comput. -Resour. Lang. CCURL European Language Resources association, Marseille, France*, 9–20.
  28. Two!Ears Team (2018). *Two!Ears Auditory Model 1.5*, Zenodo.
  29. Søndergaard, P., and Majdak, P. (2013). “The Auditory Modeling Toolbox,” In J. Blauert (Ed.), *Technol. Binaural List. Springer, Berlin-Heidelberg, Germany*, pp. 33–56.
  30. Eaton, J. W., Bateman, D., Hauberg, S., and Wehbring, R. (2016). *GNU Octave version 4.2.0 manual: a high-level interactive language for numerical computations.*
  31. Breebaart, J., van de Par, S., and Kohlrausch, A. (2001). “Binaural processing model based on contralateral inhibition III Dependence on temporal parameters,” *J Acoust Soc Am* **110**, 1105–17.
  32. Dietz, M., Lestang, J.-H., Majdak, P., Stern, R. M., Marquardt, T., Ewert, S. D., Hartmann, W. M., et al. (2018). “A framework for testing and comparing binaural models,” *Hear. Res.* **360**, 92–106.
  33. Majdak, P., Carpentier, T., Nicol, R., Roginska, A., Suzuki, Y., Watanabe, K., Wierstorf, H., et al. (2013). “Spatially Oriented Format for Acoustics: A Data Exchange Format Representing Head-Related Transfer Functions,” *Proc. 134th Conv. Audio Eng. Soc. AES Roma, Italy, Convention Paper 8880*.
  34. Wierstorf, H., Raake, A., and Spors, S. (2013). “Binaural Assessment of Multichannel Reproduction,” In J. Blauert (Ed.), *Technol. Binaural List. Springer Berlin Heidelberg, Berlin, Heidelberg*, pp. 255–278.
  35. Lindemann, W. (1986). “Extension of a binaural cross-correlation model by contralateral inhibition I Simulation of lateralization for stationary signals,” *J. Acoust. Soc. Am.* **80**, 1608–1622.
  36. Majdak, P., Goupell, M. J., and Laback, B. (2010). “3-D localization of virtual sound sources: effects of visual environment, pointing method, and training,” *Atten. Percept. Psychophys.* **72**, 454–69.
  37. Møller, H., Sørensen, M. F., Hammershøi, D., and Jensen, C. B. (1995). “Head-related transfer functions of human subjects,” *J Audio Eng Soc* **43**, 300–321.
  38. Bernstein, L. R., van de Par, S., and Trahiotis, C. (1999). “The normalized interaural correlation: Accounting for NoS $\pi$  thresholds obtained with Gaussian and “low-noise” masking noise,” *J. Acoust. Soc. Am.* **106**, 870.
  39. Baumgartner, R., Majdak, P., and Laback, B. (2016). “Modeling the Effects of Sensorineural Hearing Loss

on Sound Localization in the Median Plane,” *Trends Hear.* **20**, 2331216516662003.

40. Ziegelwanger, H., and Majdak, P. (2014). “Modeling the direction-continuous time-of-arrival in head-related transfer functions,” *J. Acoust. Soc. Am.* **135**, 1278–93.
41. Lopez-Poveda, E. A., and Meddis, R. (2001). “A human nonlinear cochlear filterbank,” *J Acoust Soc Am* **110**, 3107–18.
42. Hohmann, V. (2002). “Frequency analysis and synthesis using a Gammatone filterbank,” *Acta Acust. United Acust.* **88**, 433–442.
43. Verhulst, S., Dau, T., and Shera, C. (2012). “Nonlinear time-domain cochlear model for transient stimulation and human otoacoustic emission,” *J. Acoust. Soc. Am.* **132**, 3842–3848.
44. Zilany, M. S. A., and Bruce, I. C. (2007). “Representation of the vowel  $\$/\epsilon\$/$  in normal and impaired auditory nerve fibers: Model predictions of responses in cats,” *jas* **122**, 402–248.
45. Zilany, M. S. A., Bruce, I. C., and Carney, L. H. (2014). “Updated parameters and expanded simulation options for a model of the auditory periphery,” *J. Acoust. Soc. Am.* **135**, 283–286.
46. Dau, T., Püschel, D., and Kohlrausch, A. (1996). “A quantitative model of the ‘effective’ signal processing in the auditory system I Model structure,” *J Acoust Soc Am* **99**, 3615–22.
47. Dau, T., Kollmeier, B., and Kohlrausch, A. (1997). “Modeling auditory processing of amplitude modulation I Detection and masking with narrow-band carriers,” *J. Acoust. Soc. Am.* **102**, 2892–2905.
48. Relaño-Iborra, H., Zaar, J., and Dau, T. (2019). “A speech-based computational auditory signal processing and perception model,” *J. Acoust. Soc. Am.* **146**, 3306–3317.
49. Jepsen, M. L., Ewert, S. D., and Dau, T. (2008). “A computational model of human auditory signal processing and perception,” *J Acoust Soc Am* **124**, 422–38.
50. Ewert, S., and Dau, T. (2000). “Characterizing frequency selectivity for envelope fluctuations,” *J Acoust Soc Am* **108**, 1181–1196.
51. Viemeister, N. F. (1979). “Temporal modulation transfer functions based upon modulation thresholds,” *J. Acoust. Soc. Am.* **66**, 1364–1380.
52. Rønne, F. M., Dau, T., Harte, J., and Elberling, C. (2012). “Modeling auditory evoked brainstem responses to transient stimuli,” *J. Acoust. Soc. Am.* **131**, 3903–3913.
53. Verhulst, S., Bharadwaj, H. M., Mehraei, G., Shera, C. A., and Shinn-Cunningham, B. G. (2015). “Functional modeling of the human auditory brainstem response to broadband stimulation,” *J. Acoust. Soc. Am.* **138**, 1637–1659.
54. King, A., Varnet, L., and Lorenzi, C. (2019). “Accounting for masking of frequency modulation by amplitude modulation with the modulation filter-bank concept,” *J. Acoust. Soc. Am.* **145**, 2277–2293.
55. Dietz, M., Ewert, S. D., and Hohmann, V. (2011). “Auditory model based direction estimation of concurrent speakers from binaural signals,” *Speech Commun.* **53**, 592–605.
56. Takanen, M., Santala, O., and Pulkki, V. (2013). “Binaural assessment of parametrically coded spatial audio signals,” In J. Blauert (Ed.), *Technol. Binaural List.* Springer, Berlin, Germany, pp. 333–358.
57. Moore, B. C. J., Glasberg, B. R., and Baer, T. (1997). “A Model for the Prediction of Thresholds, Loudness, and Partial Loudness,” *J Audio Eng Soc* **45**, 224–240.
58. Glasberg, B. R., and Moore, B. C. J. (2002). “A Model of Loudness Applicable to Time-Varying Sounds,” *J*

59. Chen, Z., Hu, G., Glasberg, B. R., and Moore, B. C. J. (2011). “A new model for calculating auditory excitation patterns and loudness for cases of cochlear hearing loss,” *Hear. Res.* **282**, 69–80.
60. Moore, B. C. J., Glasberg, B. R., Varathanathan, A., and Schlittenlacher, J. (2016). “A Loudness Model for Time-Varying Sounds Incorporating Binaural Inhibition,” *Trends Hear.* , doi: 10.1177/2331216516682698.
61. Jørgensen, S., and Dau, T. (2011). “Predicting speech intelligibility based on the signal-to-noise envelope power ratio after modulation-frequency selective processing,” *J. Acoust. Soc. Am.* **130**, 1475–1487.
62. Taal, C. H., Hendriks, R. C., Heusdens, R., and Jensen, J. (2011). “An Algorithm for Intelligibility Prediction of Time-Frequency Weighted Noisy Speech,” *IEEE Trans. Audio Speech Lang. Process.* **19**, 2125–2136. Presented at the IEEE Transactions on Audio, Speech, and Language Processing.
63. Jørgensen, S., Ewert, S. D., and Dau, T. (2013). “A multi-resolution envelope-power based model for speech intelligibility,” *J. Acoust. Soc. Am.* **134**, 436–446.
64. Culling, J. F., Hawley, M. L., and Litovsky, R. Y. (2004). “The role of head-induced interaural time and level differences in the speech reception threshold for multiple interfering sound sources,” *J Acoust Soc Am* **116**, 1057–65.
65. Jelfs, S., Culling, J. F., and Lavandier, M. (2011). “Revision and validation of a binaural model for speech intelligibility in noise,” *Hear. Res.* , doi: 10.1016/j.heares.2010.12.005.
66. Hauth, C. F., Berning, S. C., Kollmeier, B., and Brand, T. (2020). “Modeling Binaural Unmasking of Speech Using a Blind Binaural Processing Stage,” *Trends Hear.* **24**, 2331216520975630.
67. Osses, A., and Kohlrausch, A. (2021). “Perceptual similarity between piano notes: Simulations with a template-based perception model,” *J. Acoust. Soc. Am.*
68. McKenzie, T., Armstrong, C., Ward, L., Murphy, D., and Kearney, G. (2021). “A Perceptually Motivated Spectral Difference Model for Binaural Signals,” *Acta Acust.*
69. Zakarauskas, P., and Cynader, M. S. (1993). “A computational theory of spectral cue localization,” *J Acoust Soc Am* **94**, 1323–1331.
70. Langendijk, E. H. A., and Bronkhorst, A. W. (2002). “Contribution of spectral cues to human sound localization,” *J Acoust Soc Am* **112**, 1583–96.
71. May, T., van de Par, S., and Kohlrausch, A. (2011). “A probabilistic model for robust localization based on a binaural auditory front-end,” *IEEE Trans Audio Speech Lang Proc* **19**, 1–13.
72. Baumgartner, R., Majdak, P., and Bernhard, L. (2013). “Assessment of sagittal-plane sound localization performance in spatial-audio applications,” In J. Blauert (Ed.), *Technol. Binaural List.* Springer, Berlin, Heidelberg, pp. 93–119.
73. Georganti, E., May, T., van de Par, S., and Mourjopoulos, J. (2013). “Sound Source Distance Estimation in Rooms based on Statistical Properties of Binaural Signals,” *Audio Speech Lang. Process. IEEE Trans. On* **21**, 1727–1741.
74. Baumgartner, R., Majdak, P., and Laback, B. (2014). “Modeling sound-source localization in sagittal planes for human listeners,” *J. Acoust. Soc. Am.* **136**, 791–802.
75. Reijniers, J., Vanderelst, D., Jin, C., Carlile, S., and Peremans, H. (2014). “An ideal-observer model of human sound localization,” *Biol. Cybern.* **108**, 169–181.

76. Kelvasa, D., and Dietz, M. (2015). “Auditory Model-Based Sound Direction Estimation With Bilateral Cochlear Implants,” *Trends Hear.*, doi: 10.1177/2331216515616378.
77. Hassager, H. G., Gran, F., and Dau, T. (2016). “The role of spectral detail in the binaural transfer function on perceived externalization in a reverberant environment,” *J. Acoust. Soc. Am.* **139**, 2992–3000.
78. Baumgartner, R., Reed, D. K., Tóth, B., Best, V., Majdak, P., Colburn, H. S., and Shinn-Cunningham, B. (2017). “Asymmetries in behavioral and neural responses to spectral cues demonstrate the generality of auditory looming bias,” *Proc. Natl. Acad. Sci.* **114**, 9743–9748.
79. Li, S., Baumgartner, R., and Peissig, J. (2020). “Modeling perceived externalization of a static, lateral sound image,” *Acta Acust.* **4**, 21.
80. Baumgartner, R., and Majdak, P. (2021). “Auditory cue combination in perceptual externalization of static sound sources: a model-based meta analysis,” *Acta Acust.*
81. Barumerli, R., Majdak, P., Baumgartner, R., Geronazzo, M., and Avenzini, F. (2021). “Predicting human spherical sound-source localization based on Bayesian inference,” *Acta Acust.*
82. McLachlan, G., Majdak, P., Reijnders, J., and Peremans, H. (2021). “Towards modelling active dynamic sound localisation based on Bayesian inference,” *Acta Acust.*
83. Hartmann, W. M., and Wittenberg, A. (1996). “On the externalization of sound images,” *J Acoust Soc Am* **99**, 3678–88.
84. Baumgartner, R., and Majdak, P. (2015). “Modeling Localization of Amplitude-Panned Virtual Sources in Sagittal Planes,” *J Audio Eng Soc* **63**, 562–569.
85. Baumgartner, R., Majdak, P., and Laback, B. (2015). “The Reliability of Contralateral Spectral Cues for Sound Localization in Sagittal Planes,” Presented at the Midwinter Meeting of the Association for Research in Otolaryngology, Baltimore, MD, USA.
86. Engel, I., and Picinali, L. (2021). “Perceptual models as a mean of assessment of Ambisonics-based binaural rendering methods,” *Acta Acust.*
87. Röttges, S., Hauth, C. F., Brand, T., and Rennie-Hochmuth, J. (2021). “Challenging a non-intrusive EC-mechanism: Modelling the Interaction between binaural and temporal speech processing,” *Acta Acust.*
88. Steidle, L., and Baumgartner, R. (2019). “Geometrical Evaluation of Methods to approximate Interaural Time Differences by Broadband Delays,” *Fortschritte Akust. Rostock*, 368–370.
89. Chacon, S., and Straub, B. (2014). *Pro git*, Apress.
90. Barnes, N. (2010). “Publish your computer code: it is good enough,” *Nature* **467**, 753.